



# Efficient Estimation of Word Representation in Vector Space

# Topics

- Language Models in NLP
- Markov Models (n-gram model)
- Distributed Representation of words
- Motivation for word vector model of data
- Feedforward Neural Network Language Model (Feedforward NNLM)
- Recurrent Neural Network Language Model (Recurrent NNLM)
- Continuous Bag of Words Recurrent NNLM
- Skip-gram Recurrent NNLM
- Results
- References

# $n$ -gram model for NLP

- Traditional NLP models are based on prediction of next word given previous  $n - 1$  words. Also known as  $n$ -gram model
- An  $n$ -gram model is defined as probability of a word  $w$ , given previous words  $x_1, x_2 \dots x_{n-1}$  using  $(n - 1)^{th}$  order Markov assumption

- Mathematically, the parameter

$$q(w|x_1, x_2 \dots x_{n-1}) = \frac{\text{count}(w, x_1, x_2 \dots x_{n-1})}{\text{count}(x_1, x_2 \dots x_{n-1})}$$

where  $w, x_1, x_2 \dots x_{n-1} \in V$  and  $V$  is some definite size vocabulary

- Above model is based on Maximum Likelihood estimation
- Probability of occurrence of any sentence can be obtained by multiplying the  $n$ -gram model of every word
- Estimation can be done using linear interpolation or discounting methods

# Drawbacks associated with $n$ -gram models

- Curse of dimensionality: large number of parameters to be learned even with the small size of vocabulary
- $n$ -gram model has discrete space, so it's difficult to generalize the parameters for that model. On the other hand, generalization is easier when the model has continuous space
- Simple scaling up of  $n$ -gram models do not show expected performance improvement for vocabularies containing limited data
- $n$ -gram models do not perform well in word similarity tasks

# Distributed representation of words as vectors

- Associate with each word in the vocabulary a distributed word feature vector in  $\mathbb{R}^m$



- A vocabulary  $V$  of size  $|V|$  will therefore have  $|V| \times m$  free parameters, which needs to be learned using some learning algorithm.
- These distributed feature vectors can either be learned in an unsupervised fashion as part of pre-training procedure or can also be learned in a supervised way as well.



# Why word vector model?

- This model is based on continuous space real variables, hence probability distribution learn by generative models are smooth functions
- Therefore unlike the  $n$ -gram models, where if a sequence of words is not present in the data corpus is not a big issue; generalization is better with this approach
- Multiple degrees of similarity : similarity between words goes beyond basic syntactic and semantic regularities. For example:  
$$\text{vector}(\text{King}) - \text{vector}(\text{Man}) + \text{vector}(\text{Woman}) \approx \text{vector}(\text{Queen})$$
$$\text{vector}(\text{Paris}) - \text{vector}(\text{France}) + \text{vector}(\text{Italy}) \approx \text{vector}(\text{Rome})$$
- Easier to train vector models on unsupervised data

# Learning distributed word vector representations

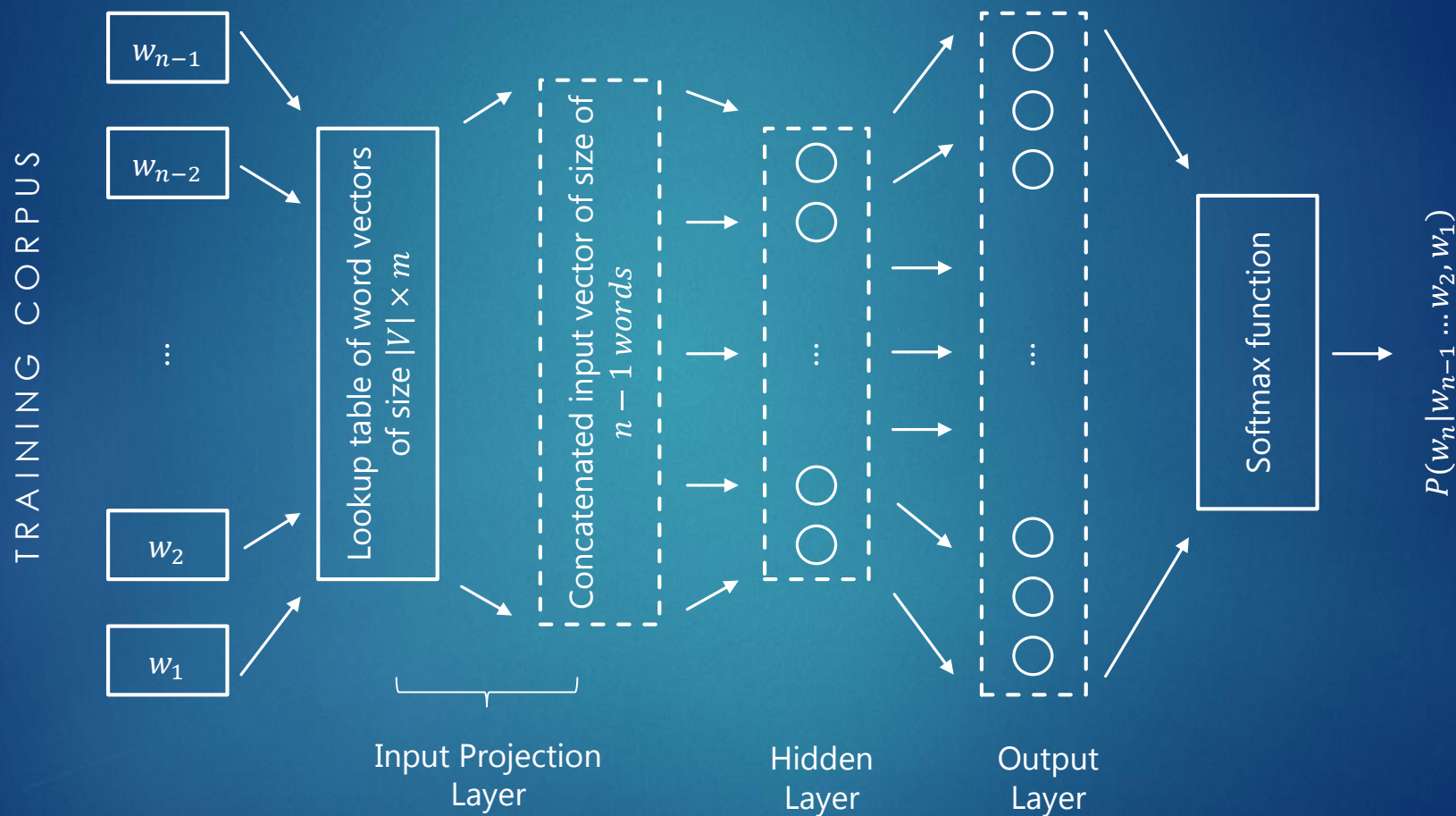
- Feedforward Neural Network Language Model : Joint probability distribution of words sequences is learned along with word feature vectors using feed forward neural network
- Recurrent Neural Network Language Models : These NNLM are based on recurrent neural networks
- Continuous Bag of Words : It is based on log linear classifier, but the input will be average of past and future word vectors. In short, here our goal is to predict word surrounding a context
- Continuous Skip-gram Model: It is also based on log linear classifier, but here it will try to predict the past and future words surrounding a given word

# Feedforward Neural Network Language Model

- Initially proposed by Yoshua Bengio et al
- It is slightly related to  $n$ -gram language model, as it aims to learn the probability function of word sequences of length  $n$
- Here input will be a concatenated feature vector of words  $w_{n-1}, w_{n-2} \dots w_2, w_1$  and training criteria will be to predict the word  $w_n$
- Output of the model will give us the estimated probability of a given sequence of  $n$  words
- Neural network architecture consists of a projection layer, a hidden layer of neurons, output layer and a softmax function to evaluate the joint probability distribution of words



# Feedforward NNLM



# Feedforward NNLM

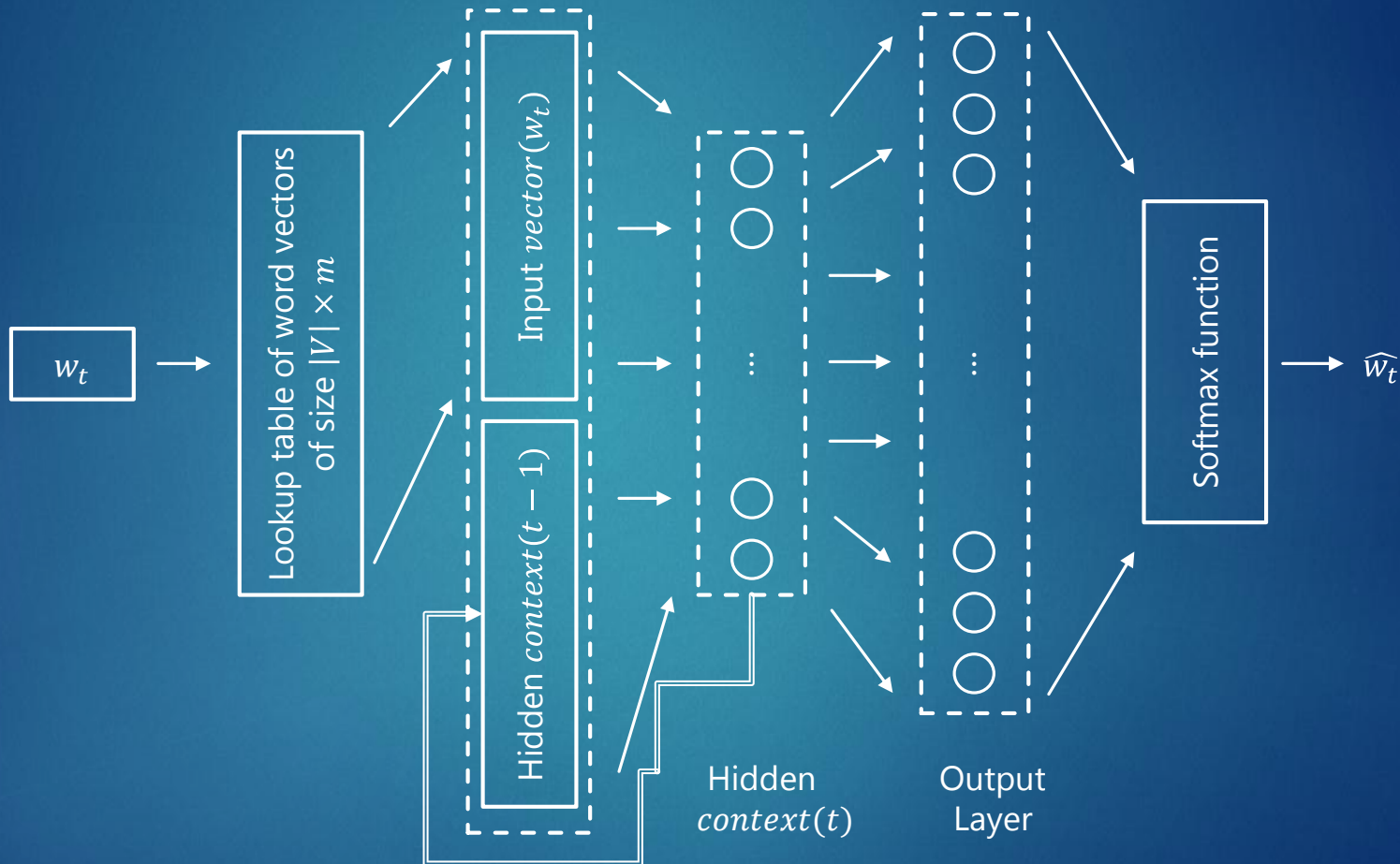
- Fairly huge model in terms of free parameters
- Neural network parameters consist of  $(n - 1) \times m \times H + H \times |V|$  parameters
- Training criteria is to predict  $n^{th}$  word
- Uses forward propagation and backpropagation algorithm for training using mini batch gradient descent
- Number of output layers in neural network can be reduced to  $\log_2 |V|$  using hierarchical softmax layers. This will significantly reduce the training time of model

# Recurrent Neural Network Language Model

- Initially implemented by Tomas Mikolov, but probably inspired by Yoshua Bengio's seminal work on NNLM
- Uses a recurrent neural network, where input layer consists of the current word vector and hidden neuron values of previous word
- Training objective is to predict the current word
- Contrary to Feedforward NNLM, it keeps on building a kind of history of previous words which got trained using the model. Therefore context window of analysis is variable here

# Recurrent NNLM

TRAINING CORPUS



# Recurrent NNLM

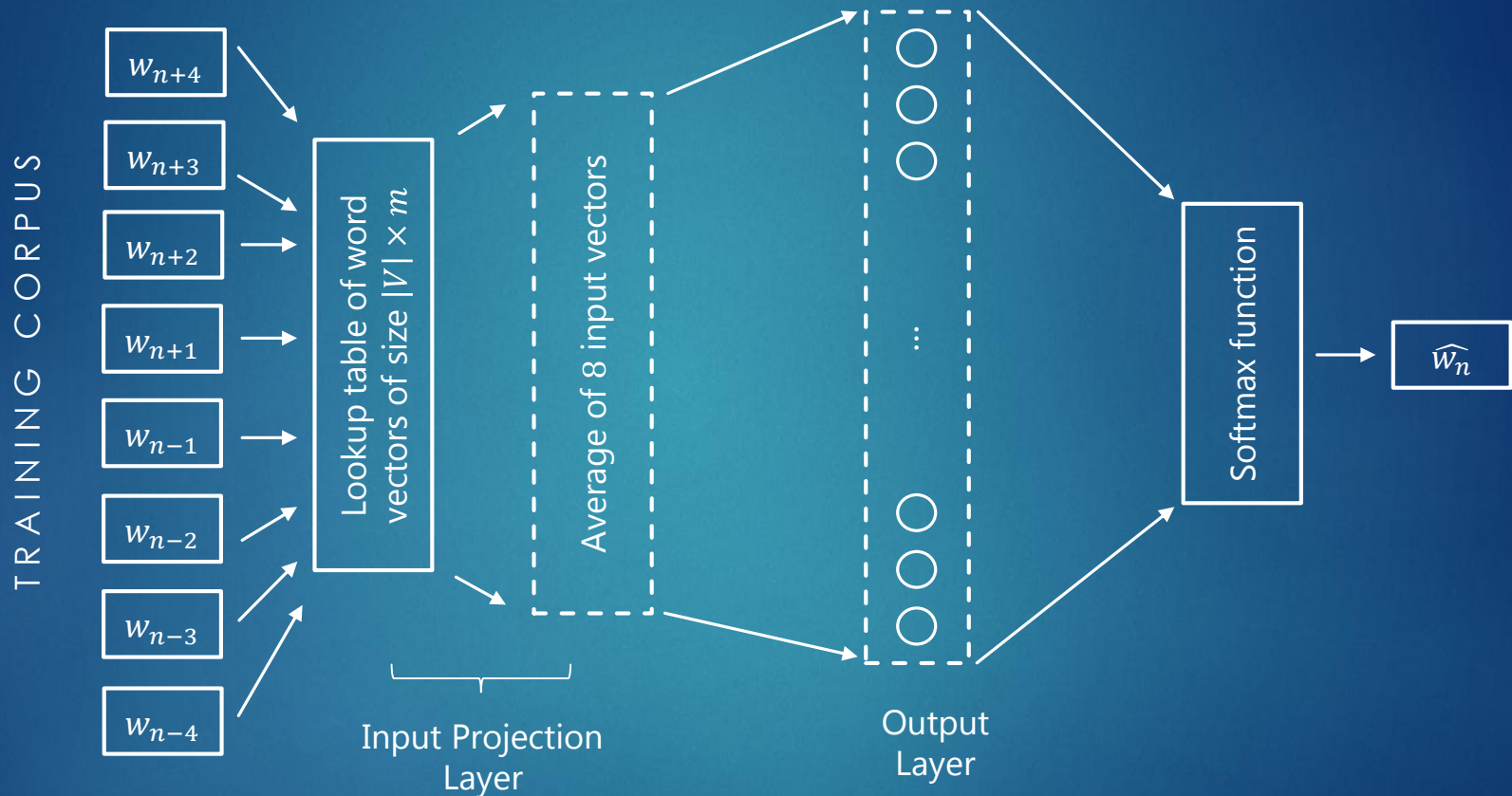
- Requires less number of hidden units in comparison to feedforward NNLM, though one may have to increase the same with increase in vocabulary size
- Stochastic gradient descent is used along with backpropagation algorithm to train the model over several epochs
- Number of output layers can be reduced to  $\log_2|V|$  using hierarchical softmax layers
- Recurrent NNLM models as much as twice reduction in perplexity as compared to  $n$ -gram models
- In practice recurrent NNLM models are much faster to train than feedforward NNLM models



# Continuous Bag of Words

- It is similar to feedforward NNLM with no hidden layer. This model only consists of an input and an output layer
- In this model, words in sequences from past and future are input and they are trained to predict the current sample
- Owing to its simplicity, this model can be trained on huge amount of data in a small time as compared to other neural network models
- This model actually does the current word estimation provided context or a sentence.

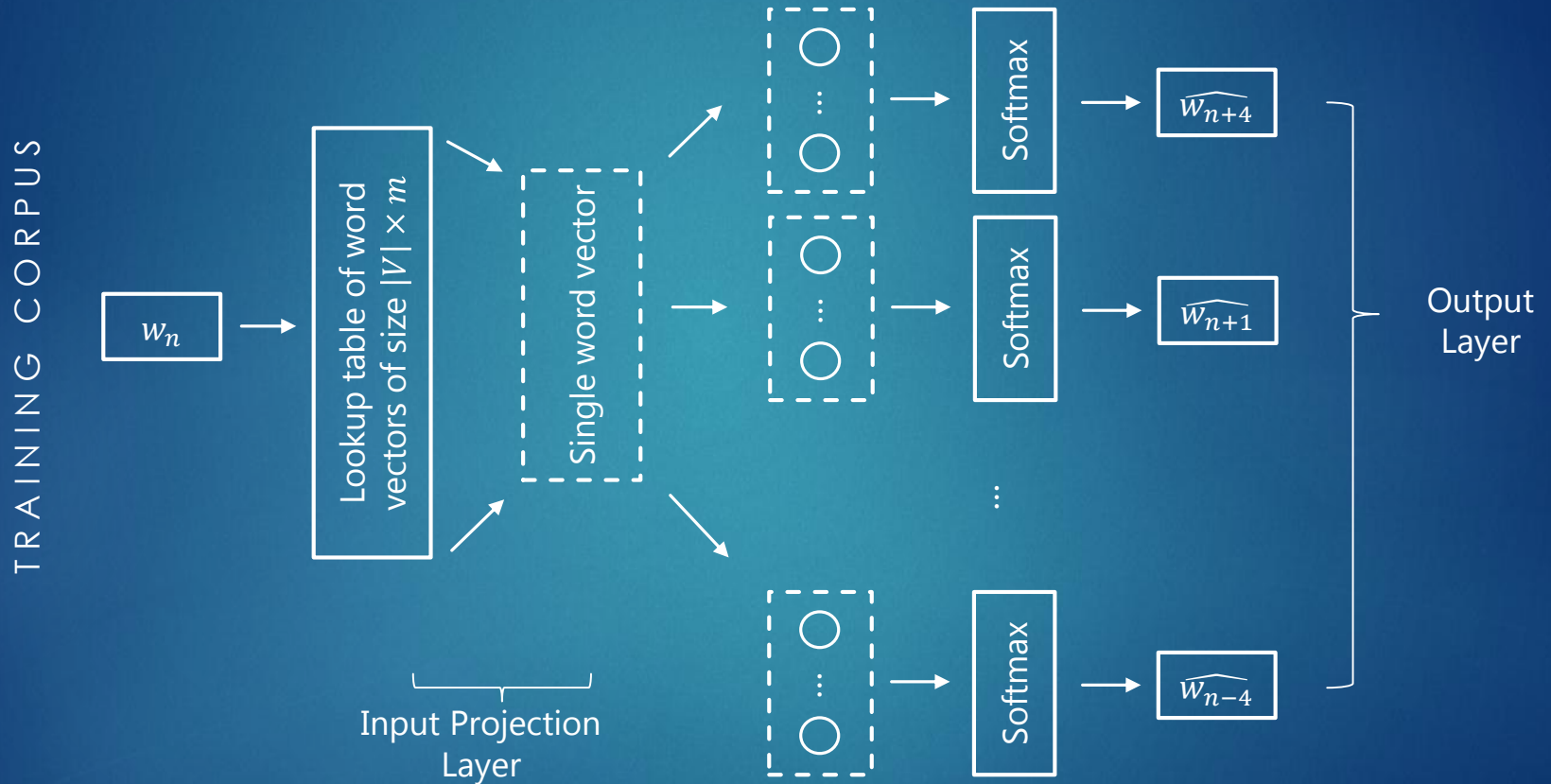
# Continuous Bag of Words



# Continuous Skip-gram Model

- This model is similar to continuous bag of words model, its just the roles are reversed for input and output
- Here model attempts to predict the words around the current word
- Input layer consists of the word vector from single word, while multiple output layers are connected to input layer

# Continuous Skip-gram Model



# Analyzing language models

- Perplexity : A measurement of how well a language model is able to adapt the underlying probability distribution of a model
- Word error rate : Percentage of words misrecognized by the language model
- Semantic Analysis : Deriving semantic analogies of word pairs, filling the sentence with most logical word choice etc. These kind of tests are especially used for measuring the performance of word vectors. For example : Berlin : Germany :: Toronto : Canada
- Syntactic Analysis : For language model, it might be the construction of syntactically correct parse tree, for testing word vectors one might look for predicting syntactic analogies such as : possibly : impossibility :: ethical : unethical



# Perplexity Comparison

	n	c	h	m	direct	mix	train.	valid.	test.
MLP1	5		50	60	yes	no	182	284	268
MLP2	5		50	60	yes	yes		275	257
MLP3	5		0	60	yes	no	201	327	310
MLP4	5		0	60	yes	yes		286	272
MLP5	5		50	30	yes	no	209	296	279
MLP6	5		50	30	yes	yes		273	259
MLP7	3		50	30	yes	no	210	309	293
MLP8	3		50	30	yes	yes		284	270
MLP9	5		100	30	no	no	175	280	276
MLP10	5		100	30	no	yes		265	<b>252</b>
Del. Int.	3						31	352	336
Kneser-Ney back-off	3							334	323
Kneser-Ney back-off	4							332	321
Kneser-Ney back-off	5							332	321
class-based back-off	3	150						348	334
class-based back-off	3	200						354	340
class-based back-off	3	500						326	<b>312</b>
class-based back-off	3	1000						335	319
class-based back-off	3	2000						343	326
class-based back-off	4	500						327	312
class-based back-off	5	500						327	312

Perplexity of different models tested on Brown Corpus

# Perplexity Comparison

Model	Weight	PPL
3-gram with Good-Turing smoothing (GT3)	0	165.2
5-gram with Kneser-Ney smoothing (KN5)	0	141.2
5-gram with Kneser-Ney smoothing + cache	0.0792	125.7
Maximum entropy model	0	142.1
Random clusterings LM	0	170.1
Random forest LM	0.1057	131.9
Structured LM	0.0196	146.1
Within and across sentence boundary LM	0.0838	116.6
Log-bilinear LM	0	144.5
Feedforward NNLM	0	140.2
Syntactical NNLM	0.0828	131.3
Combination of static RNNLMs	0.3231	102.1
Combination of adaptive RNNLMs	0.3058	101.0
ALL	1	<b>83.5</b>

Perplexity comparison of different models on Penn Treebank

# Sentence Completion Task

5-gram: IN TOKYO FOREIGN EXCHANGE TRADING YESTERDAY **THE UNIT** INCREASED AGAINST THE DOLLAR

RNNLM: IN TOKYO FOREIGN EXCHANGE TRADING YESTERDAY **THE YEN** INCREASED AGAINST THE DOLLAR

5-gram: SOME CURRENCY TRADERS SAID THE UPWARD REVALUATION OF THE GERMAN **MARK** WASN'T BIG ENOUGH AND THAT THE MARKET MAY CONTINUE TO RISE

RNNLM: SOME CURRENCY TRADERS SAID THE UPWARD REVALUATION OF THE GERMAN **MARKET** WASN'T BIG ENOUGH AND THAT THE MARKET MAY CONTINUE TO RISE

5-gram: MEANWHILE QUESTIONS REMAIN WITHIN THE E. M. S. **WEATHERED** YESTERDAY'S REALIGNMENT WAS ONLY A TEMPORARY SOLUTION

RNNLM: MEANWHILE QUESTIONS REMAIN WITHIN THE E. M. S. **WHETHER** YESTERDAY'S REALIGNMENT WAS ONLY A TEMPORARY SOLUTION

5-gram: MR. PARNES **FOLEY** ALSO FOR THE FIRST TIME **THE WIND** WITH SUEZ'S PLANS FOR GENERALE DE BELGIQUE'S WAR

RNNLM: MR. PARNES **SO LATE** ALSO FOR THE FIRST TIME **ALIGNED** WITH SUEZ'S PLANS FOR GENERALE DE BELGIQUE'S WAR

5-gram: HE SAID THE GROUP WAS **MARKET** IN ITS STRUCTURE AND NO ONE HAD LEADERSHIP

RNNLM: HE SAID THE GROUP WAS **ARCANE** IN ITS STRUCTURE AND NO ONE HAD LEADERSHIP

# Semantic Syntactic Tests

Type of relationship	Word Pair 1		Word Pair 2	
Common capital city	Athens	Greece	Oslo	Norway
All capital cities	Astana	Kazakhstan	Harare	Zimbabwe
Currency	Angola	kwanza	Iran	rial
City-in-state	Chicago	Illinois	Stockton	California
Man-Woman	brother	sister	grandson	granddaughter
Adjective to adverb	apparent	apparently	rapid	rapidly
Opposite	possibly	impossibly	ethical	unethical
Comparative	great	greater	tough	tougher
Superlative	easy	easiest	lucky	luckiest
Present Participle	think	thinking	read	reading
Nationality adjective	Switzerland	Swiss	Cambodia	Cambodian
Past tense	walking	walked	swimming	swam
Plural nouns	mouse	mice	dollar	dollars
Plural verbs	work	works	speak	speaks

# Results

Model	Vector Dimensionality	Training words	Accuracy [%]		
			Semantic	Syntactic	Total
Collobert-Weston NNLM	50	660M	9.3	12.3	11.0
Turian NNLM	50	37M	1.4	2.6	2.1
Turian NNLM	200	37M	1.4	2.2	1.8
Mnih NNLM	50	37M	1.8	9.1	5.8
Mnih NNLM	100	37M	3.3	13.2	8.8
Mikolov RNNLM	80	320M	4.9	18.4	12.7
Mikolov RNNLM	640	320M	8.6	36.5	24.6
Huang NNLM	50	990M	13.3	11.6	12.3
Our NNLM	20	6B	12.9	26.4	20.3
Our NNLM	50	6B	27.9	55.8	43.2
Our NNLM	100	6B	34.2	<b>64.5</b>	50.8
CBOW	300	783M	15.5	53.1	36.1
Skip-gram	300	783M	<b>50.0</b>	55.9	<b>53.3</b>



# Results

Model Architecture	Semantic-Syntactic Word Relationship test set		MSR Word Relatedness Test Set [20]
	Semantic Accuracy [%]	Syntactic Accuracy [%]	
RNNLM	9	36	35
NNLM	23	53	47
CBOW	24	64	61
Skip-gram	55	59	56

Different models with 640 dimensional word vectors

Model	Vector Dimensionality	Training words	Accuracy [%]			Training time [days x CPU cores]
			Semantic	Syntactic	Total	
NNLM	100	6B	34.2	64.5	50.8	14 x 180
CBOW	1000	6B	57.3	68.9	63.7	2 x 140
Skip-gram	1000	6B	66.1	65.1	65.6	2.5 x 125

Training Time comparison of different models

# Microsoft Research Sentence Completion Challenge

Architecture	Accuracy [%]
4-gram [32]	39
Average LSA similarity [32]	49
Log-bilinear model [24]	54.8
RNNLMs [19]	55.4
Skip-gram	48.0
Skip-gram + RNNLMs	<b>58.9</b>

# Complex Learned Relationships

Relationship	Example 1	Example 2	Example 3
France - Paris	Italy: Rome	Japan: Tokyo	Florida: Tallahassee
big - bigger	small: larger	cold: colder	quick: quicker
Miami - Florida	Baltimore: Maryland	Dallas: Texas	Kona: Hawaii
Einstein - scientist	Messi: midfielder	Mozart: violinist	Picasso: painter
Sarkozy - France	Berlusconi: Italy	Merkel: Germany	Koizumi: Japan
copper - Cu	zinc: Zn	gold: Au	uranium: plutonium
Berlusconi - Silvio	Sarkozy: Nicolas	Putin: Medvedev	Obama: Barack
Microsoft - Windows	Google: Android	IBM: Linux	Apple: iPhone
Microsoft - Ballmer	Google: Yahoo	IBM: McNealy	Apple: Jobs
Japan - sushi	Germany: bratwurst	France: tapas	USA: pizza

# References

- [1] Tomas Mikolov, Kai Chen, Greg Corrado, and Jeffrey Dean. Efficient Estimation of Word Representations in Vector Space. In Proceedings of Workshop at ICLR, 2013
- [2] Y. Bengio, R. Ducharme, P. Vincent. A neural probabilistic language model. Journal of Machine Learning Research, 3:1137-1155, 2003
- [3] T. Mikolov, J. Kopecky, L. Burget, O. Glembek and J. Černocký. Neural network based language models for highly inflective languages, In: Proc. ICASSP 2009